- 1. Find equations of the spheres with center (2,3,6) that touch
 - (a) the xy-plane;
 - (b) the yz-plane;
 - (c) the xz-plane.
- 2. (a) Find the acute angle between the two vectors $\mathbf{a} = \langle 4, 0, 2 \rangle$ and $\mathbf{b} = \langle 2, -1, 0 \rangle$.
 - (b) Find the acute angle between the following lines.

$$2x - y = 3$$
 $3x + y = 7$

- 3. Find the scalar and vector projections of $\mathbf{b} = \mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$ onto $\mathbf{a} = 3\mathbf{i} + 6\mathbf{j} 2\mathbf{k}$, i.e. $\mathrm{comp}_{\mathbf{a}} \, \mathbf{b}$ and $\mathrm{proj}_{\mathbf{a}} \, \mathbf{b}$.
- 4. Find two unit vectors orthogonal to both $\mathbf{u} = \langle 3, 2, 1 \rangle$ and $\mathbf{v} = \langle 1, 1, 0 \rangle$.
- 5. Find the volume of the parallelepiped ("parallelo-box") determined by the vectors $\mathbf{a} = \langle 1, 2, 3 \rangle$, $\mathbf{b} = \langle 1, 1, 2 \rangle$, $\mathbf{c} = \langle 2, 1, 4 \rangle$.
- 6. Use the scalar triple product to determine whether the points A(1,3,2, B(3,-1,6), C(5,2,0), and D(3,6,-4) lie in the same plane.
- 7. Find a vector equation and parametric equations for the line through the point (3, -4, 6) and
 - (a) perpendicular to the plane x + 3y z = 11.
 - (b) parallel to the vector $\mathbf{v} = \langle 1, 3, -1 \rangle$.
 - (c) Briefly explain why the same answer works for both parts (a) and (b).
- 8. Find a vector equation and parametric equations for the line segment from (7,3,-1) to (-2,4,5).
- 9. Find parametric equations for the line through the point (0,1,2) that is parallel to the plane x+y+z=2 and perpendicular to the line

$$x = 1 + t,$$
 $y = 1 - t,$ $z = 2t.$

- 10. Find parametric equations for the tangent line to the curve $\mathbf{r}(t) = \langle t^3 + 3t, t^2 + 1, 3t + 4 \rangle$ at the point (4, 2, 7).
- 11. Sketch the domain of the following function.

(a)
$$f(x,y) = \frac{\sqrt{y-x^2}}{1-x^2}$$

12. (a) Show that the following limit does not exist.

$$\lim_{(x,y,z)\to (0,0,0)} \frac{xy+yz^2+xz^2}{x^2+y^2+z^4}$$

(b) Show that the following limit does exist, and find the limit.

$$\lim_{(x,y)\to(0,0)} \frac{x^2+y^2}{\sqrt{x^2+y^2+1}-1}$$