

Negative angle

THROUGHOUT MATH & SUENCE:

Counter clockwise = Positive Robation)

Clockwise = NEGATIVE Robation)

THE MEASURE OF AN AUGUE (POS OR NEG) IS THE AMOUNT OF ROWHIND RECUIRED TO MOVE THE INVITAL SIDE.

#### DEGREES

 $360^{\circ}$  = 1 RENOLVION  $180^{\circ}$  =  $\frac{1}{2}$  RENOLVION  $90^{\circ}$  =  $\frac{1}{4}$  RENOLVION  $60^{\circ}$  =  $\frac{1}{6}$  RENOLVION  $45^{\circ}$  =  $\frac{1}{6}$  RENOLVION  $30^{\circ}$  :  $\frac{1}{12}$  RENOLVION

### PADIANS

27 TAO = 1 REVOLUTION

IT TAO =  $\frac{1}{2}$  REVOLUTION

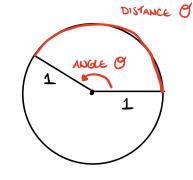
IN TAO =  $\frac{1}{4}$  REVOLUTION

IN TAO =  $\frac{1}{6}$  REVOLUTION

THE TAO =  $\frac{1}{6}$  REVOLUTION

THE TAO =  $\frac{1}{6}$  REVOLUTION

THE TAO =  $\frac{1}{12}$  REVOLUTION



THE CIRCUMFERENCE OF UNIT CIRCLE IS 27 UNITS LIMATEUR THE UNIT IS ).

THE MEASURE OF AN AUGUE IN MOIAUS IS EGNAL TO THE LENGTH OF THE COMESPONDING AND ALONG THE WINT CIRCLE.

Measure of  $\theta = 1$  rad Measure of  $\theta \approx 57.296^{\circ}$ 

#### **RELATIONSHIP BETWEEN DEGREES AND RADIANS**

$$180^{\circ} = \pi \text{ rad}$$
  $1 \text{ rad} = \left(\frac{180}{\pi}\right)^{\circ}$   $1^{\circ} = \frac{\pi}{180} \text{ rad}$ 

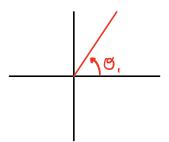
- 1. To convert degrees to radians, multiply by  $\frac{\pi}{180}$ .
- 2. To convert radians to degrees, multiply by  $\frac{180}{\pi}$ .

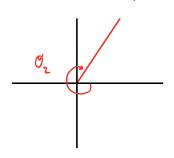
# **EXAMPLE 1** Converting Between Radians and Degrees

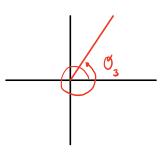
- (a) Express  $60^{\circ}$  in radians.
- **(b)** Express  $\frac{\pi}{6}$  rad in degrees.











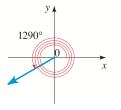
Two ANGLES IN STAND. P.K. ARE CHERNINAL IF THEIR SIDES COINCIDE.

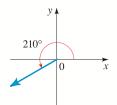
# **EXAMPLE 2** Coterminal Angles

- (a) Find angles that are coterminal with the angle  $\theta = 30^{\circ}$  in standard position.
- **(b)** Find angles that are coterminal with the angle  $\theta = \frac{\pi}{3}$  in standard position.

#### **EXAMPLE 3** Coterminal Angles

Find an angle with measure between  $0^{\circ}$  and  $360^{\circ}$  that is coterminal with the angle of measure  $1290^{\circ}$  in standard position.





**47–52** ■ Finding a Coterminal Angle Find an angle between 0 and  $2\pi$  that is coterminal with the given angle.

47. 
$$\frac{19\pi}{6}$$

48. 
$$-\frac{5\pi}{3}$$

Anc. LEWEAH

51. 
$$\frac{17\pi}{1}$$

52. 
$$\frac{51\pi}{2}$$

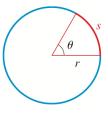


FIGURE 9 
$$s = \theta r$$

# $S = \frac{Q}{2\pi} \times CIRCUMFERENCE = \frac{Q}{2\pi} \cdot 2\pi r = rQ$

#### **LENGTH OF A CIRCULAR ARC**

In a circle of radius r the length s of an arc that subtends a central angle of  $\theta$  radians is

$$s = r\theta$$

$$\theta = \frac{s}{r}$$

# **EXAMPLE 4** Arc Length and Angle Measure

- (a) Find the length of an arc of a circle with radius 10 m that subtends a central angle of 30°.
- (b) A central angle  $\theta$  in a circle of radius 4 m is subtended by an arc of length 6 m. Find the measure of  $\theta$  in radians.

**53–62 Circular Arcs** Find the length s of the circular arc, the radius r of the circle, or the central angle  $\theta$ , as indicated.

