

* Answer Key *

Name: _____
Math 173 Introduction to Probability and Statistics

7/17/2017
Quiz 5

1. (8 points) Find the normal approximation to $P(354 \leq x \leq 359)$ for a binomial probability distribution with $n = 400$ and $p = .9$. Remember to consider the continuity correction of $x \pm .5$.

$$\mu = pn = (.9)(400) = 360$$

$$\sigma = \sqrt{pqn} = \sqrt{(.9)(.1)(400)} = 6$$

$$P(354 \leq x \leq 359) \approx P_{\text{NORM}}(353.5 \leq x \leq 359.5)$$

$$= P_{\text{NORM}}\left(\frac{353.5 - 360}{6} \leq z \leq \frac{359.5 - 360}{6}\right)$$

$$= P(z \leq -.08) - P(z \leq -1.08)$$

$$= .4681 - .1401 = \boxed{.3280}$$

2. (8 points) Suppose we assume that the temperatures of healthy humans are approximately normal with a mean of $\mu = 98.6^\circ$ and a standard deviation of $\sigma = 0.8$. If 120 healthy people are selected at random, what is the probability that the average temperature for these people is 98.3° or lower?

$$P(\bar{x} \leq 98.3) = P\left(z \leq \frac{98.3 - \mu}{\text{S.E.}}\right)$$

$$= P\left(z \leq \frac{98.3 - 98.6}{\left(\frac{.8}{\sqrt{120}}\right)}\right) = P(z \leq -4.11)$$

$\approx .0730$

$$\boxed{\approx 0}$$

CALC SATS .00001979

3. A random sample of size $n = 50$ is selected from a binomial distribution with population proportion $p = .7$.

(a) (2 points) What will be the approximate shape of the sampling distribution of $\hat{p}$?

NORMAL since $np > 5$ & $nq > 5$

(b) (4 points) What will be the mean and standard deviation (or standard error) of the sampling distribution of $\hat{p}$?

$$\text{MEAN} = p = \boxed{.7} \quad \text{S.E.} = \sqrt{\frac{pq}{n}} = \sqrt{\frac{(.7)(.3)}{50}} \approx \boxed{.0648}$$

(c) (4 points) Find the probability that the sample proportion $\hat{p}$ is less than .8.

$$\begin{aligned} P(\hat{p} < .8) &= P\left(z < \frac{.8 - p}{\text{S.E.}}\right) = P\left(z < \frac{.8 - .7}{.0648}\right) \\ &= P(z < 1.54) \approx \boxed{.9382} \end{aligned}$$

4. (8 points) A random sample of 250 children between the ages of 8 and 18 showed that 170 children had a TV in their bedroom. Estimate the proportion of all 8- to 18-year-olds who have a TV in their bedroom, and calculate the (95%) margin of error for your estimate.

$$\hat{p} = \frac{x}{n} = \frac{170}{250} = .68$$

$$\text{S.E.} = \sqrt{\frac{pq}{n}} \approx \sqrt{\frac{\hat{p}\hat{q}}{n}} = \sqrt{\frac{(.68)(.32)}{250}} \approx .0295$$

$$p \approx \hat{p} \pm 1.96 \text{ S.E.}$$

$$\begin{aligned} &\approx .68 \pm 1.96 (.0295) \approx [.6222, .7378] \\ &\text{MARGIN OF ERROR} \approx .0578 \end{aligned}$$

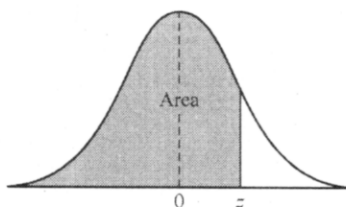


TABLE 3 Areas under the Normal Curve

<i>z</i>	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
-3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
-3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
-3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
-3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
-2.9	.0019	.0018	.0017	.0017	.0016	.0016	.0015	.0015	.0014	.0014
-2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
-2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
-2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
-2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0048
-2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
-2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
-2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
-2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
-2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
-1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
-1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
-1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
-1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
-1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
-1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0722	.0708	.0694	.0681
-1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
-1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
-1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
-1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
-0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.1611
-0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.1867
-0.7	.2420	.2389	.2358	.2327	.2296	.2266	.2236	.2206	.2177	.2148
-0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
-0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
-0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.3121
-0.3	.3821	.3783	.3745	.3707	.3669	.3632	.3594	.3557	.3520	.3483
-0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.3859
-0.1	.4602	.4562	.4522	.4483	.4443	.4404	.4364	.4325	.4286	.4247
-0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.4641

TABLE 3 (continued)

[illegible]