DATA: LIST OF n wurdens/MEASUREMENTS

 $X_1, X_2, X_3, \dots, X_n$

Example: Table 3 Entrance Examination Scores of 100 Entering Freshmen

					0				
762	451	602	440	570	553	367	520	454	653
433	508	520	603	532	673	480	592	565	662
712	415	595	580	643	542	470	743	608	503
566	493	635	780	537	622	463	613	502	577
618	581	644	605	588	695	517	537	552	682
340	537	370	745	605	673	487	412	613	470
548	627	576	637	787	507	566	628	676	750
442	591	735	523	518	612	589	648	662	512
663	588	627	584	672	533	738	455	512	622
544	462	730	576	588	705	695	541	537	563

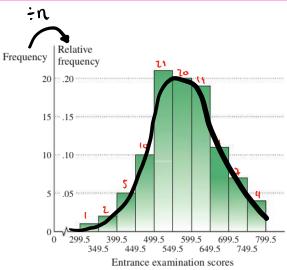
OUR GOAL IS TO EXTRACT USEFUL INFORMATION FROM THE DATA.

(DESCRIBE / SUMMARIZE)

Two METHODS: I VISUALLY

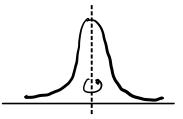
I humanially

I. VISUALLY: FREGUENCY / PRELATING FREGUENCY HISTOGRAM



NOW WE CAN SEE THE DISTRIBUTION OF MEASUREMENTS.

WONDS to DESCRIBE DISTRIBUTIONS:

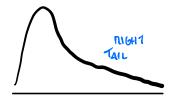


SYMMETRIC

e.g. SM Scenes

HEIGHTS OF ADULT MALES

WEIGHTS OF APPLES
Pruduced By 1 Inee

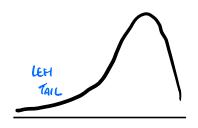


NIGHT - SKEWED

6.9. HOUSEHOLD WOME

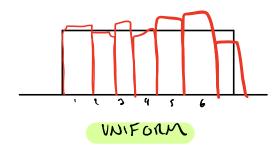
lumber of Sibungs

SIZE OF NMC AMS



LEFT - SKEWED

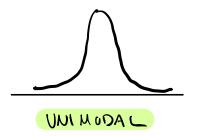
e.g. Lifetime of Humans



e.g. # TIMES EACH FACE APPEARS

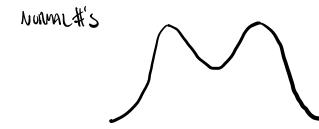
on 1000 hous of a DIE.

TIMES EACH DIGHT APPEARS IN FIRST 10 MILLION DIGHTS OF T



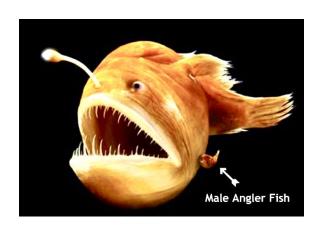
C.S. RESTING HEART TIME FOR HUMANS

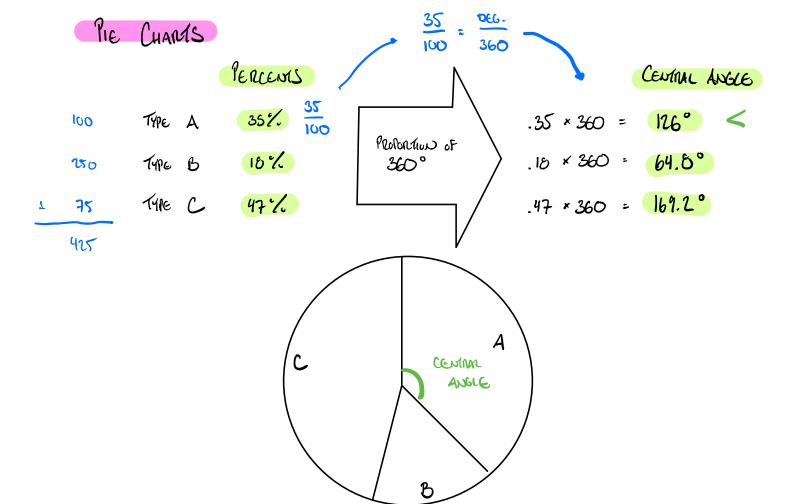
PSI Al WHICH A PARTICULAR THE OF BETCLE WHER TOBE PORS



BIMUDAL

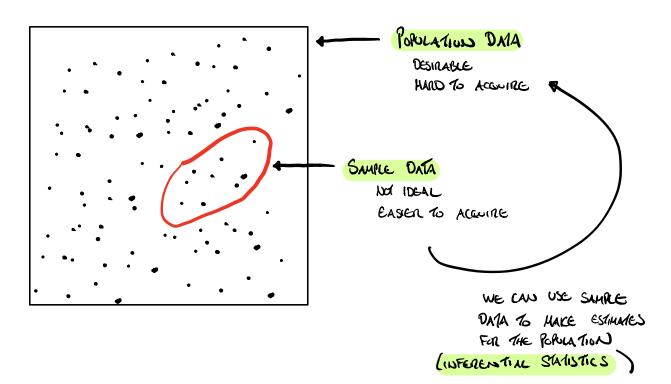
eg. Size of Anglen Fish



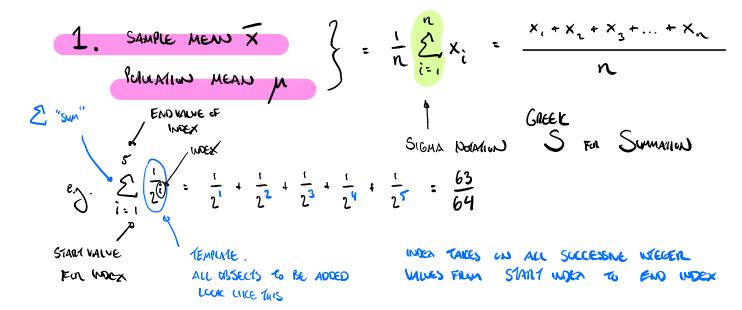


II. NUMERICALLY: MENSORS OF CENTER & VARIATION

DA/A: X, X, X, X, X, ..., Xn



3 MEASURES OF CENSICAL



The mean of 4 numbers is 90. If the mean of the first three numbers is 88, find the fourth number.

$$\frac{x_{1} + x_{2} + x_{3} + x_{4}}{4} = 90$$

$$\frac{x_{1} + x_{2} + x_{3}}{3} = 88$$

$$x_{1} + x_{2} + x_{3} + x_{4} = 4(90) = 360$$

$$x_{1} + x_{2} + x_{3} = 3(88) = 264$$

$$x_{4} = 96$$

Example. Suppose I buy 20 gallons of gas at an average price of 2.40/gallon, and you buy IO gallons of gas at an average price of 2.10/gallon. Together, what is the average price per gallon that we've paid for gas?

Connect:
$$\frac{2.10 + 2.40}{2} = \frac{1}{2}2.10 + \frac{1}{2}2.40 = 2.25$$

Connect: $\frac{7001}{7001} \frac{100}{100} = \frac{20(2.40) + 10(2.10)}{20 + 10} = \frac{20(2.40) + \frac{10}{30}2.10}{2000} = \frac{200}{100} = \frac{200}{100$

WEIGHTED AVERAGES:

Given
$$n \not = 3$$
 the average (MEAN) is

$$\frac{x_1 + x_2 + x_3 + \dots + x_n}{n} = \frac{x_1}{n} + \frac{x_2}{n} + \frac{x_3}{n} + \dots + \frac{x_n}{n}$$

$$= \frac{1}{n} x_1 + \frac{1}{n} x_2 + \frac{1}{n} x_3 + \dots + \frac{1}{n} x_n$$
ADD UP TO 1 . All the same.

Hore Generally, A weighter average of $n \not = 3$ is

$$ADD$$
 UP To 1. ALL POSITIVE.

Example. Suppose you have a homework grade of 90, and quiz grade of 85, and an exam grade of 80. If homework counts for 20% of your grade, the quiz counts for 35% of your grade, and the exam counts for 45% of your grade, calculate your average for the class.

Example. It costs a shipping company \$8.75 to ship a small package overnight. Suppose the shipping company charges a flat rate of \$19 to ship a small package overnight, and if the package is late they refund the full amount. If 93% of all packages are delivered on time, what is the average profit per package that the shipping company earns?

2. MEDIAN

Arrange the data in order from least to greatest.

If the number of measurements is odd, then the median is the number in the middle position.

If the number of measurements is even, then the median is the mean of the two numbers that share/straddle the middle position.

$$\frac{3+5}{2} = \frac{9}{4}$$

GOOD WHEN YOU DON'T WANT THE "CENTER" TO BE INFLUENCED BY EXTREME VALUES

Blood cholesterol levels. Find the mean and median for the data in the following table.

Blood Cholesterol Levels
(milligrams per deciliter)

	mingrams por a		
Michary	Interval	Frequency	MEASURGHEN
159.5	149.5–169.5	4	1-4
179.5	169.5–189.5	11	5-15
199.5	189.5–209.5	15	16 - 30
219.5	209.5–229.5	25	31-55
239.5	229.5-249.5	13	
259.5	249.5–269.5	7	
279.5	269.5–289.5	3	
299.5	289.5–309.5	2	
	/ Tota	i 60)

WE ASSUME ALL MEASUREMENTS IN EACH 1 CUSS/BIN ARE EQUAL TO THE MIDBOINT OF THM CLASS/BIN'S INTERNAL

MEAN
$$\overline{X} = \frac{1}{12} \sum_{i=1}^{60} x_i = \frac{1}{80} \left(4 \left(159.5 \right) + 11 \left(179.5 \right) + 15 \left(199.5 \right) + 16 \left$$

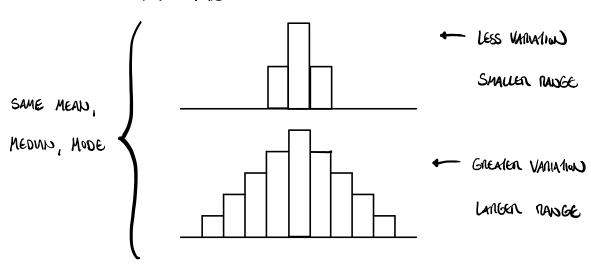
MEDIAN:

3 Mine: MOST FREQUENTLY OCCURRING MEASUREMENT (S). Yes, THERE MAY BE MUTIPLE MODES (TIES ALLOWED).

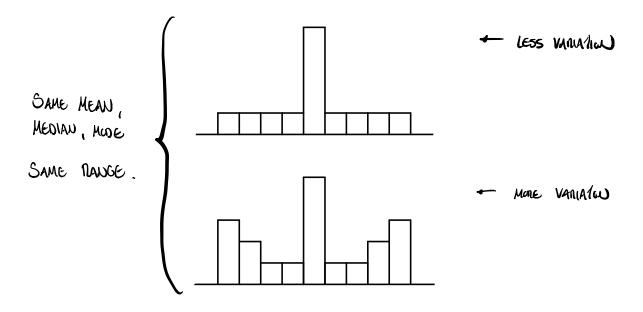
3 MEASURES OF VARIATION

"SIREAD" "VARIABILITY"

1. PLANGE = MAX - MIN



WHAT ABOUT THE FOLLOWING DISTRIBUTIONS:



WE CAN MEASURE THE DIFFERENCE IN VARIATION HERE WITH VARIABLE & STANDARD DEVIATION.

VARIANCE G2 É STANDARD DEVATION 5 FOR VORLATION DATA: X, X, X, X, X, X, X, X, VARIANCE GZ: 1 5 (x; - n) THE MEAN, SOLVIED & SCHOARD DEVIATION 5 = 75 (SOLT OF VARIANCE) VARIANCE S' É STANDARD DEVATION S FOR SAMPLE DATA: X, X2, X3, ..., Xn VARIANCE $S^2 : \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \overline{x})$ => Larger result GOOD EXTIMATES FOR SCHOARD DEVIATION S: \sign (SOLT OF VARIABLE) e.s. DATA: 13 14 17 25 26 (MEND: 19) CALCULATE THE VARIANCE & STANDARD DEVIATION ASSUMUL THE DATA COMES FROM A (a) POPULATION (b) SAMPLE (c) HOW MEASUREMENTS LIE GITHIN I STUD. DEV. OF MEAN? (d) HOW MANY MEASUREMENTS LIE GITHIN 2 STND. DEV. OF MEAN? (a) Population Variance $\sigma^2 = \frac{1}{N} \left(\frac{N}{N} \left(\frac{N}{N} - \frac{N}{N} \right)^2 \right)$ $M. G = \frac{1}{5} (150) = 30$ $x_i \mid x_i - \mu \mid (x_i - \mu)^2$ 13 G = √30 = 5.4772

(b) SAMPLE VARIABLE
$$S^2 = \frac{1}{n-1} \sum_{i=1}^{5} |x_i - \bar{x}|^2 = \frac{1}{5-1} (150)$$

$$S^2 = \frac{150}{4} = 37.5$$

Saurce standard dev.
$$S = \sqrt{S^2} = \sqrt{37.5} = 6.1237$$

In Problems 11 and 12, find the standard deviation for each set of grouped sample data using formula (5) on page 525.

11.	Interval	Frequency	
2	0.5-3.5	2	
5	3.5–6.5	5	(TUAL 15
8	6.5–9.5	7)
- 11	9.5-12.5	1	/

VARIANCE
$$S^{2} = \frac{1}{n-1} \left(\frac{3}{2!} \left(\frac{1}{x_{1}} - \frac{1}{x_{2}} \right)^{2} \right)$$

$$= \frac{2(2) + 3(5) + 7(6) + 1(11)}{15} = \frac{96}{15} = 6.4$$