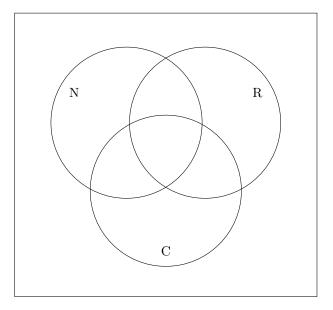
Please put away all papers, phones, smart watches, headphones, and electronic devices except a calculator. Answer all of the following questions, with answers rounded to 4 decimal places when necessary. Show enough work that it is clear how you arrived at your answer. Put a box/circle around your final answer to each question. Good luck!

- 1. Let $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$ be the universal set, and let $A = \{2, 3, 5, 7\}$ and $B = \{1, 3, 5, 7, 9\}$ be subsets of U.
 - (a) (2 points) True or false: $\emptyset \subseteq U$
 - (b) (2 points) True or false: $A \in U$
 - (c) (2 points) True of false: $B \subseteq B$
 - (d) (4 points) Find $A \cup B$.
 - (e) (4 points) Find $A \cap B'$.
 - (f) (4 points) Find $A' \cup B$.
 - (g) (6 points) List all possible subsets of $C = \{a, b, c\}$.

2.	A telephone survey of TV viewers asked participants whether or not they watch news shows	(N)	, reality
	shows (R) , and/or comedies (C) . The results are listed below.		

- 20 watch news shows
- 19 watch reality shows
- \bullet 27 watch comedies
- 19 watch comedies but not reality shows
- ullet 15 watch news shows but not reality shows
- 10 watch both news shows and comedies
- 3 watch all three
- 7 watch none of these



(a) (6 points) How many TV viewers participated in this survey?

(b) (6 points) How many TV viewers watch only comedies?

(c) (6 points) How many TV viewers do not watch comedies?

- 3. An experiment consists of randomly selecting 2 marbles (one at a time, without replacement) from a jar that initially contains 8 red marbles, 7 white marbles, and 6 blue marbles.
 - (a) (6 points) What is the probability that the first marble is red?

(b) (6 points) What is the probability that the first marble is not red?

(c) (6 points) What is the probability that the second marble is not red, given that the first marble is red?

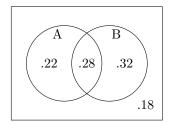
4. (6 points) The following table gives the proportion of New York City residents that live in each of the five boroughs, as well as the proportion of residnts in each borough that were born in a foreign country.

Borough	Proportion of NYC residents	Proportion born in a foreign country
Manhattan	.19	.29
Brooklyn	.31	.38
Queens	.27	.49
Bronx	.17	.32
Staten Island	.06	.21

Find the probability that a randomly selected New York City resident was born in a foreign country.

5. An experiment can result in events A, B, both A and B, or neither with the following probabilities. (Note: the chart and the Venn diagram are equivalent.)

	A	A'
B	.28	.32
B'	.22	.18



(a) (6 points) Find P(A).

(b) (6 points) Find P(A|B).

(c) (5 points) Are A and B independent? Why or why not?

(d) (5 points) Are A and B mutually exclusive (i.e. disjoint)? Why or why not?

6. Suppose that there is a test for a certain disease such that the probability that a person who has the disease tests positive is .999, and the probability that a person who does not have the disease tests positive is .015. Furthermore, suppose that the disease is rare, and the probability that a randomly selected person has the disease is only .001.(a) (6 points) What is the probability that a randomly selected person tests positive for the disease?
(b) (6 points) What is the probability that a randomly selected person has the disease, given that they
have tested positive for the disease?